

Example

items	variables (x_1, x_2)
A	(5, 3)
B	(-1, 1)
C	(1, -2)
D	(-3, -2)

→ K-means Cluster
($K=2$)

Sol? $K=2$.

(I) Arbitrary partition → (A, B), (C, D)
cluster centroid.

Cluster	Cluster centroid (\bar{x}_1, \bar{x}_2)
(A, B)	(2, 2) → C_{n1}
(C, D)	(-1, -2) → C_{n2}



(II) Compute distances from cluster centroid & reassign items (if required) to the nearest group.

A:

$$d^2(A, (A, B)) = 10$$

↑
centroid of (A, B)

$$d^2(A, (C, D)) = 61$$

↑
centroid of (C, D)

⇒ No reassignment of A is required

B:

$$d^2(B, (A, B)) = 10$$

$$d^2(B, (C, D)) = 9$$

⇒ B reassignment required, B is closer to (C, D) than to (A, B)

⇒ Reassign B to cluster (C, D)

→ (A, (B, C, D))

III) →
Update of Cluster Centroid

III

Clusters	centroids (\bar{x}_1, \bar{x}_2)
(A)	(5, 3)
(B, C, D)	(-1, -1)

Step IV) Squared distance to group cluster

items.

Cluster	A ✓	B ✓	C ✓	D ✓
(A)	0	40	41	89
(B, C, D)	52	4	5	5

⇒ NO reassignment is required further

Termination step process.

⇒ (A), & (B, C, D) are the desired clusters.